

B TECH
(SEM-VI) THEORY EXAMINATION 2017-18
DIGITAL SIGNAL PROCESSING

*Time: 3 Hours**Max. Marks: 100*

Note: Attempt all the sections. Assume missing data suitably, if any.

SECTION-A**1. Attempt all of the following questions:****(2×10=20)**

- (a) If $x(n) = \{6, 5, 4, 3\}$ what will be $x((2-n))_4$.
- (b) What is the DFT of $\delta(n)$?
- (c) What is the equation for order of Butterworth filter?
- (d) What is difference between IIR and FIR filter?
- (e) Write Gibbs phenomena.
- (f) Define Time Reversal of a sequence in DFT.
- (g) What is twiddle factor in DFT?
- (h) Write the frequency transformation rule for the conversion of LP to HP filter.
- (i) What is the difference between circular convolution and linear convolution?
- (j) Write the expression for hamming window.

SECTION-B**2. Attempt any three of the following questions:****(3×10=30)**

- (a) Use the 4 point DFT and IDFT to determine circular convolution of the following sequence:

$$x(n) = \{1, 2, 3, 1\}$$

$$h(n) = \{4, 3, 2, 2\}$$

- (b) Determine the 8-point DFT of the following sequence using DIF FFT algorithm:

$$x(n) = \{1, 2, 3, 4\}$$

- (c) Write a short notes on the following:

(i) Butterfly Computation (ii) Inplace Computation (iii) Bit reversal

- (d) Use bilinear transformation to convert low pass filter, $H(s) = 1/s^2 + \sqrt{2}s + 1$ into a high pass filter with pass band edge at 100 Hz and $F_s = 1$ kHz.

- (e) Design a digital Butterworth filter that satisfied the following constraints, using Impulse invariant Transformation.

$$0.9 \leq H(e^{j\omega}) \leq 1 \quad 0 \leq \omega \leq \frac{\pi}{2}$$

$$H(e^{j\omega}) \leq 0.2 \quad \frac{3\pi}{4} \leq \omega \leq \pi$$

SECTION – C

3. Attempt any one of following questions: (1×10=10)

- (a) (i) A system function is given as under:

$$H(z) = \frac{(1 + 8z^{-1} + 6z^{-2})}{(1 + 8z^{-1} + 12z^{-2})}$$

realize the system function using ladder structure.

- (ii) State and prove the circular convolution theorem.

- (b) Design a linear phase FIR (high pass) filter of order seven with cutoff frequency $\frac{\pi}{4}$ radian/ sec using Hanning window.

4. Attempt any one of following questions: (1×10=10)

- (a) Determine the circular convolution of the following sequences and compare the results with linear convolution:

$$x(n) = (1, 2, 3, 4)$$

$$h(n) = (1, 2, 1)$$

- (b) The first five point of the 8-point DFT of a real valued sequence are:

$\{0.25, 0.125 - j0.3018, 0, 0.125 - j0.0518, 0\}$. Determine the remaining three points.

5. Attempt any one of following questions: (1×10=10)

- (a) The system function of the analog filter is given as :

$$H(s) = \frac{s+0.1}{(s+0.1)^2 + 16}$$

Obtain the system function of digital filter using bilinear transformation which is resonant at $\omega_r = \frac{\pi}{2}$

- (b) Design an FIR filter to meet the following specifications:

Pass band edge = 2 kHz

Stop band edge = 5 kHz

Stop band attenuation = 42 dB

Sampling frequency = 20 kHz

Use Hanning window.

6. Attempt any one of following questions: (1×10=10)

- (a) Obtain the direct form I, direct form II, cascade and parallel form realization for the following system:

$$y(n) = -0.1 y(n-1) + 0.2 y(n-2) + 3 x(n) + 3.6 x(n-1) + 0.6 x(n-2)$$

- (b) Find the inverse DFT of the sequence :

$$X(k) = \{6, -2+j2, -2, -2-j2\}, \text{ using DIT-FFT algorithm.}$$

7. Attempt any one of following questions: (1×10=10)

- (a) What are the different window functions used for windowing? Explain the effect of using different window functions for designing FIR filter on the filter response.

- (b) Derive and draw the flow graph for DIF FFT algorithm for N=8.