

B. TECH.**THEORY EXAMINATION (SEM–VI) 2016-17****DIGITAL SIGNAL PROCESSING****Time : 3 Hours****Max. Marks : 100****Note : Be precise in your answer. In case of numerical problem assume data wherever not provided.****SECTION – A****1. Attempt the following questions:****10 x 2 = 20**

- (a) Define digital signal processing.
- (b) Draw the block diagram of digital signal processing.
- (c) Explain the basic elements required for realization of digital system.
- (d) Define linear convolution and its physical significance.
- (e) What is the fundamental time period of the signal $x(t) = \sin 15\pi t$.
- (f) Draw a transformation matrix of size 4x4 and explain the properties of twiddle factor.
- (g) Differentiate between IIR and FIR filters
- (h) Enumerate the Advantages of DSP over ASP.
- (i) Write the expression for computation efficiency of an FFT.
- (j) Calculate the DFT of the sequence $s(n) = \{1, 2, 1, 3\}$.

SECTION – B**2. Attempt any five of the following questions:****5 x 10 = 50**

- (a) Obtain the Parallel form realization for the transfer function $H(z)$ given below:

$$H(z) = \frac{2 + z^{-1} + \frac{1}{4} z^{-2}}{(1 + \frac{1}{2} z^{-1})(1 + z^{-1} + \frac{1}{2} z^{-2})}$$

- (b) Calculate the DFT of $x(n) = \cos an$
- (c) Drive and draw the flow graph for DIF FFT algorithm for $N=8$.
- (d) Determine $H(z)$ using the impulse invariant technique for the analog system function

$$H(s) = \frac{1}{(s + 0.5)(s^2 + 0.5s + 2)}$$

- (e) Determine $H(z)$ for a Butterworth filter satisfying the following constraints

$$\sqrt{0.5} \leq \begin{cases} |H(e^{j\omega})| \leq 1 & 0 \leq \omega \leq \frac{\pi}{2} \\ |H(e^{j\omega})| \leq 0.2 & \frac{3\pi}{4} \leq \omega \leq \pi \end{cases}$$

with $T=1\text{sec}$. Apply impulse invariant transformation.

- (f) Given $x(n) = 2^n$ and $N=8$ find $X(K)$ using DIT FFT algorithm. Also calculate the computational reduction factor.
- (g) Design a low-pass filter with the following desired frequency response

$$H_d(e^{j\omega}) = \begin{cases} e^{-j2\omega}, & -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4} \\ 0, & \frac{\pi}{4} < |\omega| < \pi \end{cases} \quad \text{and using window function}$$

$$w(n) = \begin{cases} 1, & 0 \leq n \leq 4 \\ 0, & \text{otherwise} \end{cases}$$

- (h) Convert the analog filter with system function $H(s) = \frac{s+0.1}{(s+0.1)^2+9}$ into digital filter with a resonant frequency of $\omega_r = \frac{\pi}{4}$ of using bilinear transformation.

SECTION – C

Attempt any two of the following questions:

2 x 15 = 30

- 3** (i) Obtain the ladder structure for the system function $H(z)$ given below.

$$H(z) = \frac{2 + 8z^{-1} + 6z^{-2}}{1 + 8z^{-1} + 12z^{-2}}$$

- (ii) Compute the Circular convolution of two discrete time sequences $x_1(n) = \{1, 2, 1, 2\}$ and $x_2(n) = \{3, 2, 1, 4\}$

- 4** (a) Determine the 4-point discrete time sequence from its DFT $X(k) = \{4, 1-j, -2, 1+j\}$
 (b) Explain the following phenomenon: (i) Gibbs Oscillations, (ii) Frequency wrapping
- 5** (a) Derive the relation between DFT and Z-transform of a discrete time sequence $s(n)$.
 (b) Design a digital Chebyshev filter to satisfy the constraints

$$\begin{aligned} 0.707 \leq |H(e^{j\omega})| \leq 1 & \quad 0 \leq \omega \leq 0.2\pi \\ |H(e^{j\omega})| \leq 0.1, & \quad 0.5\pi \leq \omega \leq \pi \end{aligned}$$

Using bilinear transformation with $T=1s$